A Geometric Brownian Motion Car-Following Model: Towards a Better Understanding of Capacity Drop

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ABSTRACT
When traffic congestion forms on a road, the flow downstream of the congestion is generally lower than the pre-queue capacity. This phenomenon is called the capacity drop. Recent empirical observations show a positive relationship between the speed in congestion and the queue discharge rate. In literature, this relation is also observed in the absence of lane changing. These findings help in understanding the microscopic mechanism behind the capacity drop. Literature indicates that variations in driver behaviors can account for the capacity drop. However, to the best of authors’ knowledge, there is no solid understanding of what and how this variation in driver behaviors lead to the capacity drop, especially without lane changing. Hence, this paper fills in this gap. We extend the parsimonious car-following model (Laval et al. 2014) by incorporating the empirically observed desired acceleration stochasticity. The extended parsimonious car-following model shows different capacity drop magnitudes in different traffic situations, consistent with empirical observations. Data collected from a car-following experiment is applied to validate the model, which shows the new model can catch most of the properties of longitudinal behaviors. All results indicate that the stochasticity of desired accelerations is a significant reason for the capacity drop. The new insights can be used to develop and test new measures in traffic control.

KEYWORDS
traffic flow; capacity drop; car-following model; intra-driver variation

1. Introduction

It is generally agreed that the capacity drop phenomenon is the salient feature of freeway bottlenecks: once congestion occurs, the queue discharge rate is 5-20\% lower than the pre-queue capacity (Hall and Agyemang-Duah 1991; Banks 1991; Cassidy and Bertini 1999; Srivastava and Geroliminis 2013; Chung et al. 2007; Cassidy and Rudjanakanoknad 2005). Recent empirical findings by Yuan et al. (2015) show yet another reproducible phenomenon, that the queue discharge rate increases with the speed in the queue; see Figure 1. In this figure, the capacity drop magnitude is around 26\% when the vehicular speed in congestion is zero km/h and decreases as the vehicular speed increases.

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speed increases. The mechanisms behind this “speed-capacity” relationship are not well understood, to the detriment of traffic operations, simulation models and traffic delay calculations. This paper aims to fill this void.

Laval and Daganzo (2006) demonstrate that the disruption caused by some lane-changing maneuvers near merge and moving bottlenecks might explain capacity drop; see also Yeo (2008); Coifman and Kim (2011); Leclercq et al. (2011, 2015); Yuan et al. (2017b, 2015). This disruption takes the form of a void in traffic in front of the lane-changing vehicle, which is caused by the bounded acceleration of the maneuver.

However, recent observations reveal that capacity drop can also take place in the absence of lane changing (Oh and Yeo 2015). This suggests that voids can form between any two successive vehicles rather than only in the front of lane changers. After analyzing time headways in the downstream free-flow state of congestion in the absence of lane changing, Oh and Yeo (2015) also find that the queue discharge rate decreases as the congestion severity increases, which is consistent with the speed-capacity relationship from Yuan et al. (2015). It has been argued that the driver-vehicle-combination (DVC) heterogeneity might explain this phenomenon. Wong and Wong (2002) suggested that the variance of drivers’ desires for free-flow speeds might be a reason for the capacity drop. They extend the LWR model (Lighthill and Whitham 1955; Richards 1956) to incorporate a distribution of fundamental diagrams characterized by their choices of speeds in a traffic stream, and obtain a reverse-lambda fundamental diagram within simulations. However, a behavioral explanation and empirical data for this conjecture are still lacking. Chen et al. (2016) study the effect of heavy vehicles on driver behaviors through empirical analysis and find that heavy vehicles might reduce capacity drop by stabilizing surrounding traffic streams, but caution that more data is needed to confirm their findings. Coifman (2015) show the impacts of the DVC heterogeneity on the fundamental diagram, but no conclusion on the capacity drop is drawn.

Two other mechanisms have been proposed for explaining capacity drop (see Yuan
et al. 2017a, for a summary): inter-driver spread (Papageorgiou et al. 2008) and the intra-driver variation (Tampère 2004; Zhang and Kim 2005; Treiber et al. 2006; Chen et al. 2014; Yuan et al. 2017a). The inter-driver spread means heterogeneity in the desired accelerations, e.g. voids can be created between a low-acceleration vehicle and its high-acceleration predecessor, as noted in Laval and Daganzo (2006). Yuan et al. (2017a) find that the queue discharge rate reduction due to the acceleration spread is rather small compared to the bounded acceleration component.

The intra-driver variation mechanism means that the capacity drop is a result of traffic condition dependent variable driver behavior. For example, Zhang and Kim (2005) assume the driver gap-time as a function of both gap-distance and traffic phase. Treiber et al. (2006) investigate an adaption of desired time headway as a function of local speed variances. However, in these models, a proper understanding of the capacity drop from a behavioral perspective is missing. The timid-aggressive models (Laval and Leclercq 2010; Chen et al. 2014, 2012a,b) modify Newell’s first-order car-following model (Newell 2002) to incorporate both bounded accelerations and different reaction patterns to disturbances to replicate realistic oscillations formation and propagation. The drawback of this formulation is that several extra parameters are needed, which might be difficult to estimate in real applications. Laval et al. (2014) propose a stochastic extension to Newell’s car-following model with bounded accelerations requiring a single extra parameter and exhibiting a predicted ability similar to the timid/aggressive models.

Based on the above discussions, it seems reasonable that the parsimonious model in Laval et al. (2014) might explain the speed-capacity relationship in Figure 1. Unfortunately, this is not the case as shown in Figure 2. The inability of the model in Laval et al. (2014) to reproduce the bottlenecks speed-discharge rate relationship raises the question whether the stochasticity in driver behaviors is associated with the capacity drop phenomenon, and if so, in which way. In this paper, we answer this question by showing an alternative formulation of the model in Laval et al. (2014) based on additional empirical data analysis. An explicit driver behavioral mechanism behind the capacity drop phenomenon is developed here, which is expected to shed light on traffic operations. Towards this end, the outline of the paper is as follows: we present
the extended car-following model in Section 2. The power of the car-following model over showing longitudinal drivers’ behaviors is investigated in Section 3, with comparisons to earlier empirical findings. Section 3 simulates the capacity drop and its relation with congestion states using the extended model. Finally, we end this paper with conclusions and discussions in Section 4.

2. The car-following model

This section formulates the proposed car-following model, which is based on the concept of desired acceleration. The desired acceleration is defined as the acceleration drivers are willing to impose on their vehicles in the absence of a leader.

Figure 3 shows the desired acceleration at different vehicular speeds. These data include 15 acceleration processes by the same driver, which are collected only when the test vehicle is the first one in a platoon stopped in front of the red signal. The data is the same as analyzed in Laval et al. (2014). Figure 3(b) shows that the standard deviation of the desired accelerations almost reduces linearly as the vehicular speed grows. The points in Figure 3(b) are given by calculating the standard deviation of an aggregation of points in an interval of 3 m/s. This observed dependency between standard deviation and speed was overlooked in the model proposed in Laval et al. (2014), and we will see that it might be the reason why this model cannot capture the speed-capacity relationship. One may argue that using a linear function to fit the trend shown in Figure 3 may not be accurate. But we would argue that the overall decreasing trend shown in Figure 3 is consistent with real driving features as observed in Allen et al. (2000), and is a key ingredient to predict realistic traffic dynamics. In the future, to what extent the linearity assumption might influence the results should be investigated.

We now show that this stochastic feature during accelerating is relevant for reducing queue discharge rates, and can be incorporated into the model by using a geometric Brownian motion to describe desired accelerations. We firstly introduce a stochastic desired acceleration model that is consistent with empirical data in Section 2.1, and...
then it is incorporated into Newell’s first-order car-following framework in Section 2.2. Finally, a single-parameter model is given in Section 2.3.

### 2.1. The desired acceleration model

In this section we formulate the desired acceleration model, which corresponds to the acceleration processes of a single driver on an empty road, only constrained by the engine power and the way the driver uses it. Using empirical data, Laval et al. (2014) show that the following linear vehicle kinematics model is a good approximation for the mean desired acceleration $E[a(v)]$ when a vehicle is traveling at speed $v(t)$ at time $t$, i.e.:

$$E[a(v(t))] = (v_f - v(t))\beta$$

where $v_f$ is the free-flow speed and $\beta$ is a positive parameter with units of $[\text{time}]^{-1}$. (1) is also consistent with linearized relaxation acceleration model in Treiber et al. (2000, 2006). Laval et al. (2014) assume that the desired acceleration is normally distributed around this mean with constant standard deviation, $\text{Std}[a(v(t))]$, independent of the speed. However, we found that further analysis of the empirical data in that reference reveals that $\text{Std}[a(v(t))]$ decreases with the speed $v(t)$; this is shown in Figure 3(b). It can be seen that the mean and standard deviation are linear functions of the speed, both of which vanish near $v_f$. This suggests that the following stochastic differential equation (SDE) should be a good approximation:

$$d v(t) = (v_f - v(t))\beta dt + (v_f - v(t))\sigma dW(t)$$

where $W(t)$ is the standard Brownian motion and $\sigma$ is diffusion coefficient, which has units of $[\text{time}]^{-1/2}$. Using $S(t) = v_f - v(t)$, we reformulate (2) into:

$$dS(t) = -S(t)(\beta dt + \sigma dW(t))$$

with initial conditions $S(0) = S_0$, with $S_0 = v_f - v_0$ and $v_0 = v(0)$. It is noted that in simulations, the initial state is the state in the last simulation instant rather than the traffic condition at the beginning of the simulation. That is, as shown in Zhang et al. (2012) and Wu et al. (2014), similar to the many existing car-following models, the car-following model in this paper takes the current traffic states into account.

SDE (3) indicates that the stochastic process $S(t)$ follows a Geometric Brownian motion, and therefore, under Itô’s interpretation of SDEs (Øksendal 2010), obeys a log-normal distribution with expected value $E[S(t)] = S_0e^{-\beta t}$ and variance $\text{Var}[S(t)] = S_0^2e^{-2\beta t}(e^{\sigma^2 t} - 1)$. Hence, $v(t)$ follows log-normal distribution with $E[\cdot]$ and $\text{Var}[\cdot]$ given by:

$$E[v(t)] = v_f - (v_f - v_0)e^{-\beta t}$$

$$\text{Var}[v(t)] = (v_f - v_0)^2(e^{-(2\beta - \sigma^2) t} - e^{-2\beta t})$$

Note that log-normality here means that $v(t)$ is always non-negative. To identify the parameters that drive the model, consider the dimensionless quantities $\tilde{\sigma}^2 = \sigma^2/\beta$. 
\[ \tilde{t} = \beta t \text{ and } \tilde{v} = v/v_f, \] which simplify (4) into:

\[ E[\tilde{v}(\tilde{t})] = 1 - (1 - \tilde{v}_0)e^{-\tilde{t}} \]

\[ \text{Var}[\tilde{v}(\tilde{t})] = (1 - \tilde{v}_0)^2(e^{-(2-\tilde{\sigma}^2) \tilde{t}} - e^{-2\tilde{t}}) \]

which reveals that apart from the initial data \( \tilde{v}_0 \) the only parameter in the model is \( \tilde{\sigma}^2 \). Notice how the steady-state speed variance tends to zero if \( \tilde{\sigma}^2 \leq 2 \) (and to infinity otherwise), which should always be the case in practice as we will see momentarily.

2.2. Incorporation into car-following framework

Here we incorporate the desired acceleration model (4) into the Newell's first order car-following framework (Newell 2002). Newell's model can be expressed as:

\[ x_{i+1} = \min\{x_{i+1}(t-\tau) + \tau v_f, x_i(t-\tau) - \delta\} \]

where \( \delta = 1/\rho_j \), \( x_i(t) \) is the location of vehicle \( i \) at time \( t \) and \( \tau = 1/(w \rho_j) \) is the wave travel time between two successive vehicles. The jam density \( \rho_j \), shock wave speed \(-w\) and free-flow speed \( v_f \) are three parameters of a triangular flow-density fundamental diagram, from which the capacity and critical density associated with the fundamental diagram can be derived.

Remark here the speed generation via (4) or (5) in this research may result in a speed higher than the free-flow speed \( v_f \). To incorporate the \( v(t) \) in to (6), the term \( \tau v_f \) is reformulated into \( \tau \cdot \min(v_f, v_{i+1}(t)) \). That is:

\[ x_{i+1}(t) = \min\{x_{i+1}(t-\tau) + \tau \cdot \min(v_f, v_{i+1}(t)), x_i(t-\tau) - \delta\} \]

where the \( v_{i+1}(t) \) term in (7) is obtained by generating a log-normal random number with mean value and variance given by (4). Recall that the log-normal distribution ensures \( v(t) \) is always non-negative. The formulation of (7) may make an assumption that the acceleration vanishes at free-flow, which might be not fully realistic. Readers can relax this assumption by formulating (7) as \( x_{i+1}(t) = \min\{x_{i+1}(t-\tau) + \tau \cdot v_{i+1}(t), x_i(t-\tau) - \delta\} \) which allows \( v_{i+1}(t) > v_f \).

2.3. A single-parameter model

It is important to note that it has been shown that, in the context of the kinematic wave model, the parameters added by the fundamental diagram (\( \tau, v_f \) and \( \delta \) in our case) do not impact flow or delay calculations, when expressed in dimensionless form (Laval et al. 2014; Daganzo and Knoop 2016; Laval and Chilukuri 2016).

It follows that that capacity drop should be a function of \( \tilde{\sigma}^2 \) alone, since we have seen that this is the only additional parameter required by our model. The numerical experiments in the next section confirm this result.

3. Simulation experiments

This section presents two simulation experiments with the proposed model. The results are consistent with empirical data, at the aggregate level. In both cases the experiment
Figure 4. Samples of vehicular trajectories in car-following experiments. The experiments have been reported in (Jiang et al. 2014, 2015). Without lane changing, oscillations can be observed. The subfigure at the right corner of each figure shows the formation and the development of oscillations.

consists of a platoon on a single lane and without lane changes.

The triangular fundamental diagram has parameters $w = 18 \text{ km/h}$, $v_f = 114 \text{ km/h}$, and free-flow capacity $C = 2280 \text{ veh/h}$. Accordingly, $\rho_j \approx 146.7 \text{ veh/km}$ and critical density $\rho_{cri} = 20 \text{ veh/km}$.

3.1. Platoon oscillation growth

Empirical data show that the standard deviation of vehicular speeds in a platoon with a constant-speed leader increases along the platoon in a concave way. This “concavity” in the oscillation growth was first revealed in a 25-vehicle car-following platoon experiment (Jiang et al. 2014); Figure 4 shows two sample experiments. Tian et al. (2016) used both Jiang’s and NGSIM trajectory data and found that when the leader speed is in between 30-55 km/h, the oscillation growth is well approximated by a single concave function. These findings are consistent with Li and Ouyang (2011), who show that oscillation amplitude exhibits a similar growth pattern. But this reference also shows that as of vehicle number increases oscillation amplitude standard stabilizes, something not seen in Jiang’s data.

Our simulation experiment consists of a 250-vehicle platoon on a one-lane road. The platoon leader drives at a constant speed $v_{lead}$, which is set to be 30 km/h, 40 km/h and 50 km/h in different simulations. For each value of $v_{lead}$, we run 500 simulations, each for $T = 300\tau$ long. For comparison purposes, we use different values of $\beta$ and $\sigma$.

At time $t = 0$, all vehicles are driving in a congested state with an equilibrium spacing $1/\rho_0$. $\rho_0$ is the density in the congestion. That is, $v_i(0) = w(\rho_j - \rho_0)/\rho_0$, $i = 1, 2, \ldots, 250$.

The sample trajectories in Figure 5 show how several oscillations develop and grow. Figure 6 shows the relation between the vehicle number and the distribution of speed standard deviation obtained from the 500 simulation runs. The $v_{lead}$ increases from Figure 6(a) to Figure 6(c). It can be seen that the standard deviation of vehicular speed increases in a concave curve along the platoon when the car number is small, e.g. smaller than 100. As the vehicle number increases, the standard deviation of speed flattens out around a fixed value, which itself increases with $v_{lead}$. The good match with empirical data is apparent.

Figure 7 shows how the standard deviation of oscillatory series $\hat{x}(t) = x(t) - \bar{x}(t)$ propagate along the platoon. $\hat{x}(t)$ can be seen as the Newell’s trajectory. A growing-
Figure 5. Samples of vehicular trajectories in simulations. The color map indicates the vehicular speed. \( v_{\text{lead}} = 50 \text{ km/h} \) in this sample. An overview of the simulation results are given in (a). The trajectories in the rectangle in (a) is shown in (b) for a better visualization. In simulations, \( \beta = 0.06 \) and \( \sigma = 0.06 \).

Figure 6. Concavity revealed in car-following platoon simulations when the leading vehicle in the platoon drives at (a) \( v_{\text{lead}} = 30 \text{ km/h} \), (b) \( v_{\text{lead}} = 40 \text{ km/h} \) and (c) \( v_{\text{lead}} = 50 \text{ km/h} \). We used \( \beta = 0.06 \) and \( \sigma = 0.055 \). The shaded areas illustrate the 95%-percentage (between 97.5\(^{\text{th}}\) and 2.5\(^{\text{th}}\) percentile) and 66%-percentage (between 83\(^{\text{th}}\) and 17\(^{\text{th}}\) percentile) of the 500 simulations. The bold curve is the mean value of the simulation results. The dots in Figure 6 are the speed standard deviation obtained from Jiangs’ car-following experiments.
Figure 7. Standard deviation of oscillatory series revealed in car-following platoon simulations when the leading vehicle in the platoon drives at (a) $v_{\text{lead}} = 30 \text{ km/h}$, (b) $v_{\text{lead}} = 40 \text{ km/h}$ and (c) $v_{\text{lead}} = 50 \text{ km/h}$. In simulations, $\beta = 0.06$ and $\sigma = 0.055$.

and-flattening pattern can be observed, which is consistent with Li and Ouyang (2011). In addition, we observed that the standard variance of the oscillatory series stabilize at a fixed value, which is with $v_{\text{lead}}$.

3.2. Speed-capacity relationship

In this section, we study to what extent the proposed model can reproduce the speed-capacity relationship observed in Yuan et al. (2015); Oh and Yeo (2015). As observed in Oh and Yeo (2015), the queue discharge rate reduction in absence of lane changing is a large proportion of the reduced capacity at bottlenecks, outperforming the reduction due to lane changing.

The simulation setup in this section is identical to the previous sections. But the leading vehicle which drives at a low constant speed $v_{\text{lead}}$, is removed, allowing vehicles in the queue to accelerate.

Figure 8 shows two sample runs from our simulations. It can be seen that as vehicles accelerate voids appear within the platoon, which propagate indefinitely downstream, causing the capacity drop. To measure this drop, we calculate the queue discharge flow $q_{\text{dis}}$ per:

$$q_{\text{dis}} = \frac{(N - 1) v_f}{\sum_{i=2}^{N} s_i(T)}$$

where $s_i(T)$ is vehicle $i$’s spacing at the simulation ending time $T$, and $N$ is the number of vehicles in the platoon. A dimensionless queue discharge rate $\tilde{q}_{\text{dis}}$ is used in coming analysis, with unit $C$. We selected $N = 450$ since we observed that the discharge rate stabilizes at that point; see Figure 9(a).
Figure 8. Sample trajectories from our simulations. The color map indicates the vehicular speed. The speed at $t = 0$ is (a) $v_j = 50$ km/h (or density $\rho_0 = 39$ veh/km) and (b) $v_j = 0$ km/h (or density $\rho_0 = \rho_j \approx 146.7$ veh/km). $N = 50$ vehicles, excluding the virtual vehicle, are simulated on a one-lane road segment.

Figure 9. Simulation results by means of observed queue discharge rates as a function of parameter $N$ and $\tilde{\sigma}^2$.

Figure 9(b) shows the queue discharge rate is a decreasing linear function of $\tilde{\sigma}$. A decreasing function is as expected because the larger the viability of the acceleration processes, the larger the voids in the traffic stream; linearity is somewhat surprising.

Finally, Figure 10 shows that the proposed model produces a speed-capacity relationship that is consistent with empirical data. Notice that if $\tilde{\sigma}^2 = 0.06$, the capacity drop can reach around 22% with a wide moving jam (i.e., $v_j = 0$ km/h), which is similar to the capacity drop magnitude empirically observed in Yuan et al. (2015) and Yuan et al. (2017a).

4. Conclusions and discussions

There are two relevant contributions in this work. Firstly, this paper for the first time proposes a longitudinal behavior-oriented interpretation - desired acceleration errors - to explain the capacity drop. Though numerous car-following models in literature have been able to reproduce the queue discharge rate reduction and (possibly) even the speed-capacity relation, we argue that the approach used in those models lacks
a connection with driver behavior. That is, a profound behavioral mechanism which can even interpret the mechanisms (as introduced in Section 1) proposed in those previous car-following models is desirable. Our first contribution is such an attempt. It is worthwhile to notice that the desired acceleration error mechanism originates from empirical observations.

Secondly, this paper extended the parsimonious car-following model in Laval et al. (2014) to reproduce empirical speed-capacity relationships. This was achieved by modeling driver acceleration errors as a Geometric Brownian motion, which is consistent with our empirical data showing that the standard deviation of the desired acceleration is a decreasing function of the speed. It is worthwhile to notice that the desired acceleration error mechanism seems to be operational nowadays. The possible implications for traffic management are discussed in this section later.

Notably, the extended model remains a single-parameter model if one is interested in flow or delay calculations; in particular, the speed-capacity relationship depends on a single parameter, $\tilde{\sigma}^2 = \sigma^2/\beta$. Similarly, the queue discharge rate was found to be a decreasing linear function of $\tilde{\sigma}$. From the driver behavior perspective, this parameter encapsulates human error, $\sigma^2$ and how fast acceleration changes with speed, $\beta$. Therefore, queue discharge rates can be increased by (i) decreasing human error as much as possible, especially at the beginning of the acceleration process, and/or (ii) increasing the acceleration at low speeds, by increasing engine power and/or educating drivers to be more aggressive when accelerating from a full stop.

Based on these findings, firstly we can argue that newer vehicle technologies should be beneficial for reducing or maybe even eliminating capacity drop. Autonomous vehicles should be able to substantially reduce the variability of acceleration processes, which is consistent with (i) above; electric vehicles offer much greater accelerating power than conventional combustion engine vehicles, especially at lower speeds, which accords well with (ii). Secondly, the roadside traffic management can also gain benefits from our findings, which again differs from previous car-following models. Let us give an example. Yuan et al. (2015) show a lane drop on A4 in the Netherlands where serious congestion have been observed for several days. If we set a speed limit - say 70 km/h - in the downstream of the lane drop, then we believe that the queue discharge rate can be increased since the $\beta$ increases which decreases the $\tilde{\sigma}$. In Figure 11, the
capitals indicate the traffic state downstream of the lane-drop bottleneck, while the lower cases indicate the congested state upstream. Without the speed limit, the queue discharge rate corresponds to state “A” and “a”. When speed limit is conducted, in Figure 11 the free-flow speed decreases from $v_{OA}$ to $v_{OB}$ ($v_{OA}$, $v_{OB}$ and $v_{OC}$ is the slope of line OA, OB and OC, respectively), the queue discharge rate increase from $q_a$ to $q_b$, $q_b$ and $q_c$ correspond to state “a”, “b” and “c” respectively. Finally, when the speed limit reduces to $v_{OC}$ when the flow in state $C$ equals $q_c$, we believe that $v_{OC}$ can be the optimal speed limit.

It is worthwhile to notice that the fundamental diagram used in this study is triangular. One may argue that the triangular fundamental diagram is an approximation rather than reality. But the shape of the fundamental diagram will not influence the acceleration model at all. In the acceleration model, the only parameter associated to the fundamental diagram is the free-flow speed which will be given in a FD with any shapes.

We used the comprehensive car-following experiment in Jiang et al. (2014) to show that the model also captures the “concavity” in traffic flow. Further analysis is needed to investigate if concavity in our model also depends on the fundamental diagram parameters, and if it is able to produce the periods and amplitudes of oscillations observed in the data. More data calibrations and validations of the model in freeway environment are desirable. These topics are currently being investigated by the authors (e.g., in Xu and Laval (2018)).

The desired acceleration model (see Section 2.1) developed in this paper can be incorporated into the OVM (Optimal Velocity Model) or IDM (Intelligent Driver Model) car-following model in a straightforward way when describing the acceleration on a free road from a standstill (i.e., we don’t need to use the adaptation time in the IDM and OVM car-following model. Readers are referred to Treiber and Kesting (2013) for descriptions on the OVM and IDM car-following model).

The primary interest of this research is in the longitudinal driving behavioral mechanism behind the capacity drop. The model developed in this paper contributes to validating the proposed mechanism. In the future, to what extent this model can reproduce or/and explain other traffic phenomena should be investigated. Moreover, for operation more consideration of the uncertainty and stochasticity in traffic flow should be desirable.
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